

Name: \_\_\_\_\_

Grade: \_\_\_\_\_

Score: \_\_\_\_\_

## Worksheet #5



### ANGLE RELATIONSHIPS AND RATIO PROBLEMS

**Learning goal:** Students will Master solving angle problems using ratios and algebraic equations.

1. If angles  $A:B = 2:3$  and together they form a right angle, find the value of  $2A - B$ .

2. Angles  $P$  and  $Q$  are in the ratio  $1:2$ . If they together form a straight angle, find the value of  $2P - Q$ .

3. Two angles are in the ratio  $5:7$  and form a straight angle. Find the value of  $B - A$ .

4. Two angles are in the ratio  $2:3$  which is  $40$  degrees less than right angle. What is the measure of two angles?

5. Angle  $A$  is one-third of angle  $B$ . Together, they form a straight angle. Find the measure of each angle.

6. A reflex angle and an acute angle sum up to a full circle. If the acute angle is  $45^\circ$ , find the reflex angle.

7. One angle is  $50^\circ$  more than the other. Together they form a straight angle. Find both angles.

8. Angles  $P$  and  $Q$  are in the ratio  $1:2$ . If they together form a right angle, find the value of  $Q - P$ .

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## Worksheet #5 (Answers)

**ANGLE RELATIONSHIPS AND RATIO PROBLEMS**

**Learning goal:** Students will Master solving angle problems using ratios and algebraic equations.

1. If angles  $A:B = 2:3$  and together they form a right angle, find the value of  $2A - B$ .

**Solution:**  $A + B = 90^\circ$

Let  $A = 2x$ ,  $B = 3x$

$2x + 3x = 90 \Rightarrow 5x = 90 \Rightarrow x = 18$

$A = 2 \times 18 = 36$ ,  $B = 3 \times 18 = 54$

$2A - B = 2 \times 36 - 54 = 72 - 54$

$2A - B = 18$

2. Angles  $P$  and  $Q$  are in the ratio  $1:2$ . If they together form a straight angle, find the value of  $2P - Q$ .

**Solution:**  $P + Q = 180^\circ$

$x + 2x = 180 \rightarrow 3x = 180 \rightarrow x = 60$

$P = x = 60^\circ$ ,  $Q = 2x = 120^\circ$

$2P - Q = 120 - 120 = 0$

$2P - Q = 0$

3. Two angles are in the ratio  $5:7$  and form a straight angle. Find the value of  $B - A$

**Solution:**

$A + B = 180^\circ$

$5x + 7x = 180 \rightarrow 12x = 180 \rightarrow x = 15$

$A = 75^\circ$ ,  $B = 105^\circ$

$B - A = 105 - 75 = 30$

4. Two angles are in the ratio  $2:3$  which is  $40$  degrees less than right angle. What is the measure of two angles?

**Solution:**

$2x + 3x = 90^\circ - 40^\circ = 50^\circ$

$5x = 50 \rightarrow x = 10$

$2x = 20^\circ$ ,  $B = 30^\circ$

Therefore, 2 angles are  $20^\circ$  and  $30^\circ$

5. Angle  $A$  is one-third of angle  $B$ . Together, they form a straight angle. Find the measure of each angle.

**Solution:**

Let angle  $A = x$ , then angle  $B = 3x$

$x + 3x = 180 \rightarrow 4x = 180 \rightarrow x = 45$

$A = 45^\circ$ ,  $B = 135^\circ$

Final Answer:  $A = 45^\circ$ ,  $B = 135^\circ$

6. A reflex angle and an acute angle sum up to a full circle. If the acute angle is  $45^\circ$ , find the reflex angle.

**Solution:**

Reflex angle = Full circle - acute angle

$= 360^\circ - 45^\circ$

$= 315^\circ$

7. One angle is  $50^\circ$  more than the other. Together they form a straight angle. Find both angles.

**Solution:**

Let smaller angle =  $x$ , larger =  $x + 50$

$x + x + 50 = 180 \rightarrow 2x = 130$

$x = 65$

Angles =  $65^\circ$ ,  $115^\circ$

8. Angles  $P$  and  $Q$  are in the ratio  $1:2$ . If they together form a right angle, find the value of  $Q - P$ .

**Solution:**

$P + Q = 90$

$x + 2x = 90 \rightarrow 3x = 90$

$x = 30$

$P = 30^\circ$ ,  $Q = 60^\circ$

$Q - P = 60 - 30 = 30$